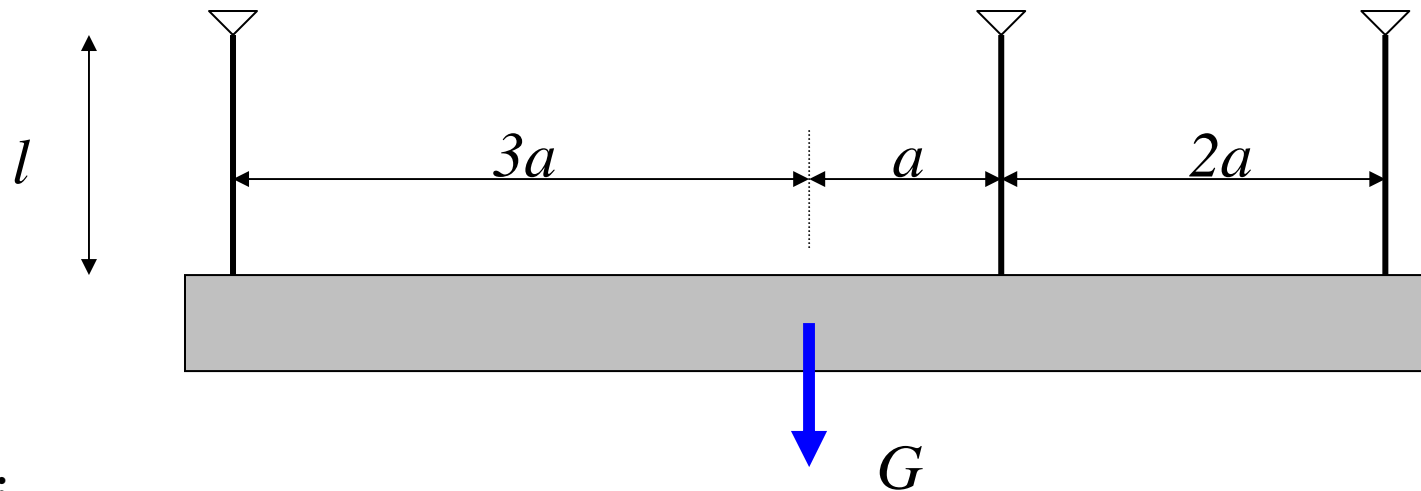


ELASTIC versus PLASTIC ANALYSIS

STRUCTURE IN TENSION



Given:

- Cross sectional area of each cable : $A=100 \text{ mm}^2$, length $l=0,5 \text{ m}$, $a=0,5 \text{ m}$
- Yield stress of the cable material : $f_y = 235 \text{ N/mm}^2$
- Youngs modulus of the cable material : $E=2,1 \cdot 10^5 \text{ N/mm}^2$

Questions:

- Find the value of G for first occurrence of the yield stress (elastic limit)
- Find the failure load of G

ANSWER : ELASTIC LIMIT

Analysis:

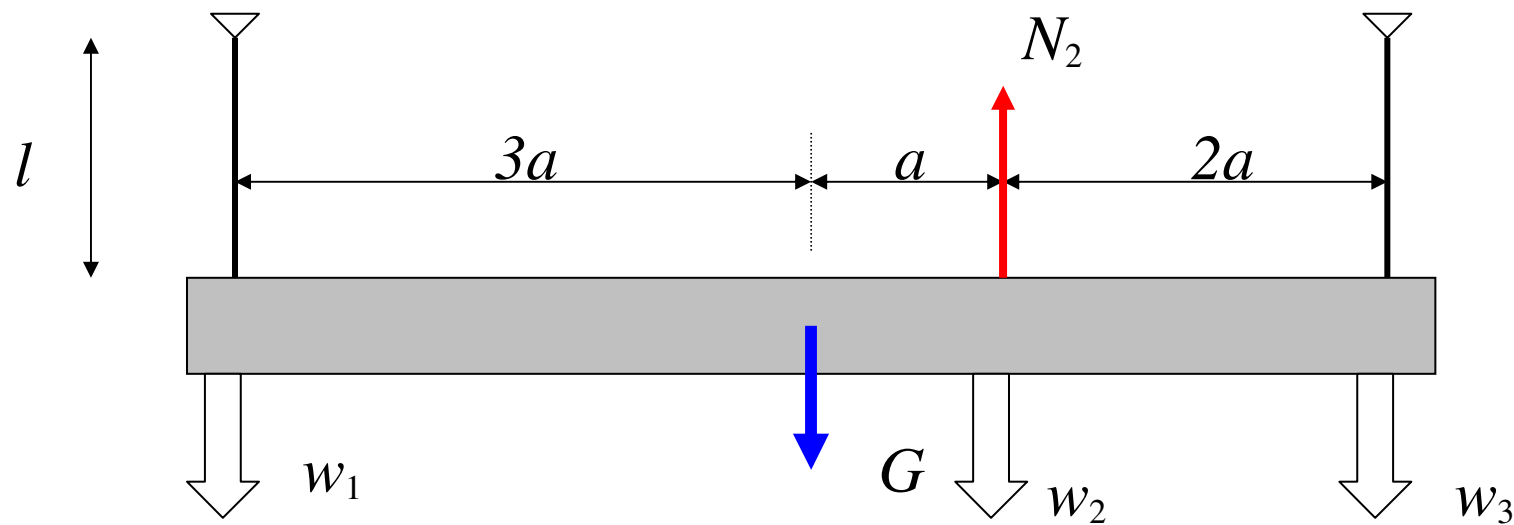
- *three* unknown cable forces
- *two* equilibrium conditions which can be used ($\Sigma V=0$, $\Sigma T=0$)

Static undeterminate structure to the degree of one

Solution strategy: Force Method

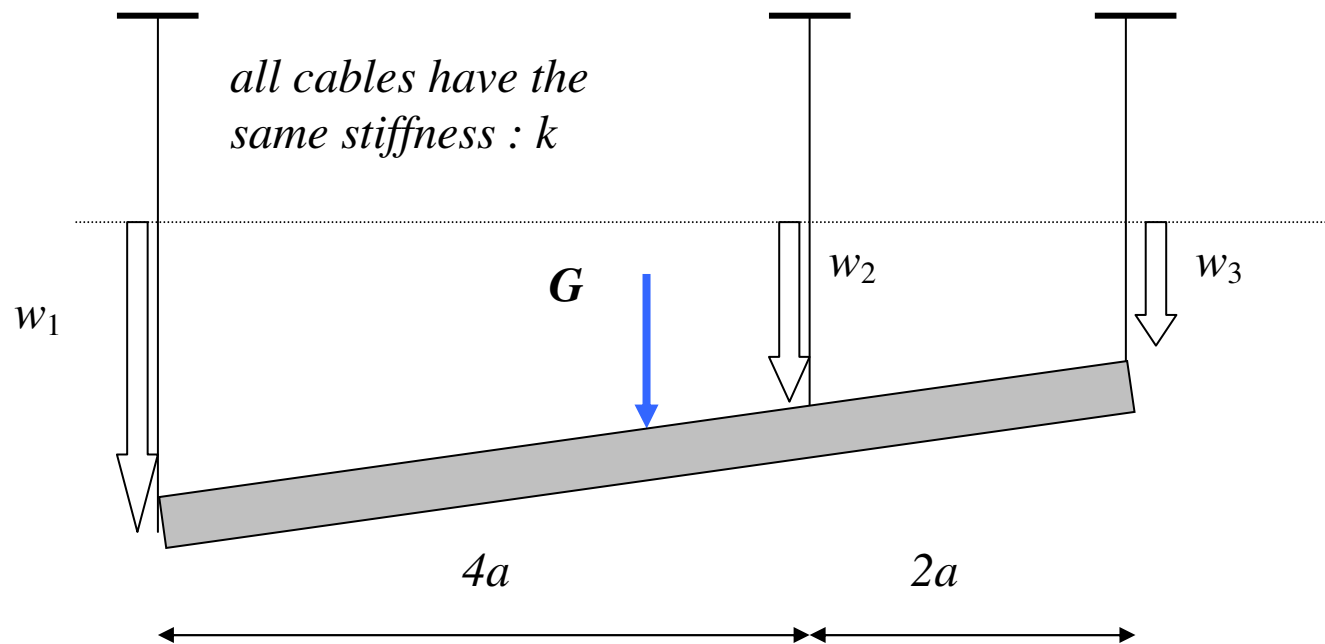
- Chose a static redundant(force in one of the cables)
- Reduce the structure to a static determinate system
- Setup the compatibility demand which belongs to the redundant force
- Solve the unknown
- Find the maximum cable force which is not allowed to exceed the elastic limit N_p

STATIC DETERMINATE PRINCIPAL SYSTEM WITH STATIC REDUNDANT



stiffness of the cable: $k = \frac{EA}{l}$

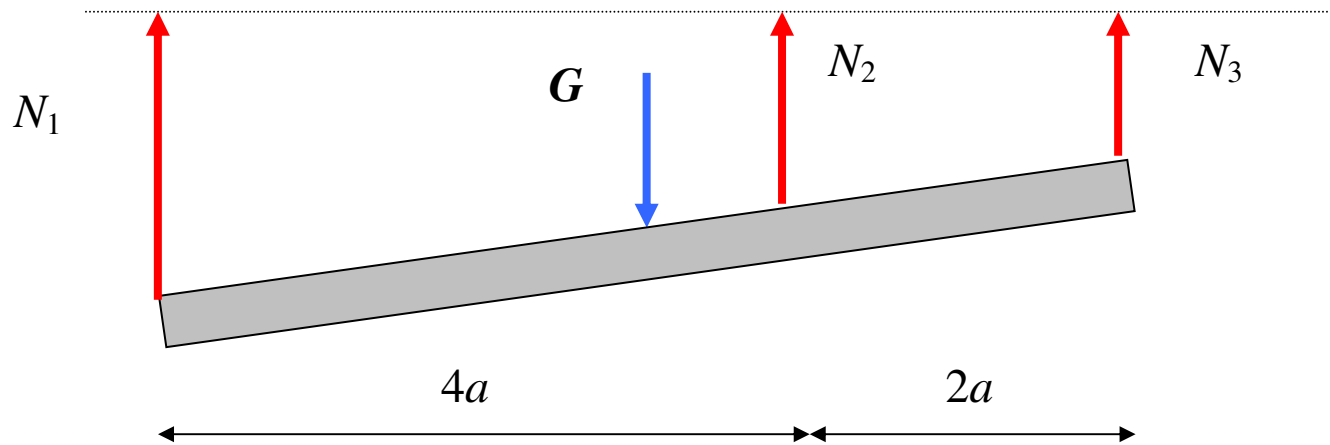
COMPATIBILITY CONDITION



$$w_2 = w_1 - \left(\frac{w_1 - w_3}{6a} \right) \cdot 4a$$

$$w_2 = \frac{1}{3} (w_1 + 2w_3) \quad \Rightarrow \quad N_2 = kw_2 = \frac{1}{3} k(w_1 + 2w_3) = \frac{1}{3} N_1 + \frac{2}{3} N_3$$

RESULTING SYSTEM OF EQUATIONS



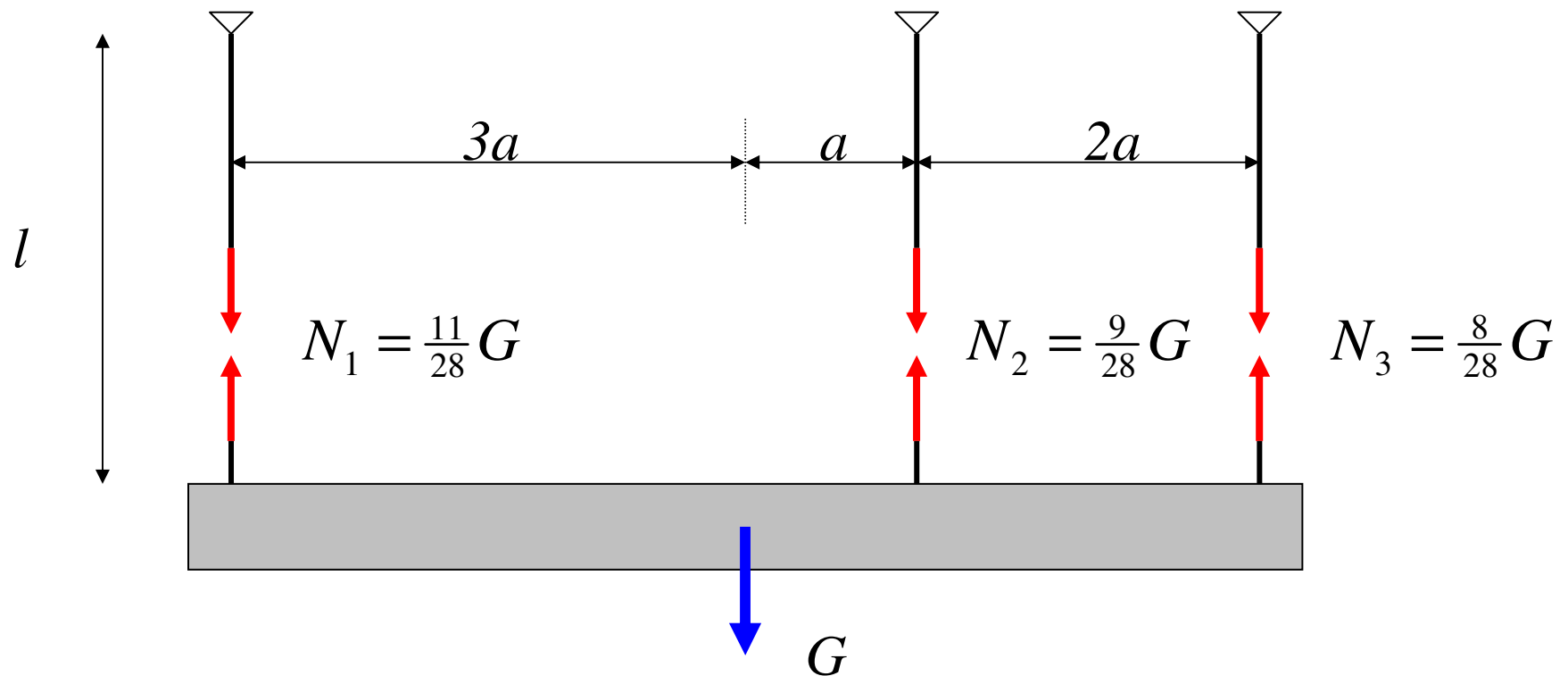
$$\begin{aligned} N_1 + N_2 + N_3 &= G \\ N_1 \cdot 3a - N_2 \cdot a - N_3 \cdot 3a &= 0 \\ N_1 - 3N_2 + 2N_3 &= 0 \end{aligned} \Rightarrow \begin{bmatrix} 1 & 1 & 1 \\ 3 & -1 & -3 \\ 1 & -3 & 2 \end{bmatrix} \begin{Bmatrix} N_1 \\ N_2 \\ N_3 \end{Bmatrix} = \begin{Bmatrix} G \\ 0 \\ 0 \end{Bmatrix}$$

$$\begin{aligned} N_p &= A \cdot f_y = 23,5 \times 10^3 \text{ N} \\ N_p &= 23,5 \text{ kN} \end{aligned}$$

$$N_1 = \frac{11}{28} G ; N_2 = \frac{9}{28} G ; N_3 = \frac{8}{28} G$$

$$G_e = \frac{28}{11} \cdot N_p = 59,8 \text{ kN}$$

ELASTIC CABLE FORCE DISTRIBUTION



ANSWER : FAILURE LOAD

Analysis:

- *failure* occurs if an additional load can not be taken by the structure, end of load capacity
- *two* cables which will yield results in a mechanism therefore failure occurs when the second cable starts to yield

Solution strategy :

- Incremental method or
- Direct method based upon failure mechanism

(this is shown in class)