

**Problem : Work & Energy****( approx. 40 min )**

A linear elastic beam with bending stiffness  $EI$  is split in to two parts which are linked with a rotational spring with spring stiffness  $r$ . The beam is partially loaded with a distributed load  $q$  as indicated in the figure. All dimensions are also specified. Axial and shear deformation are neglected.

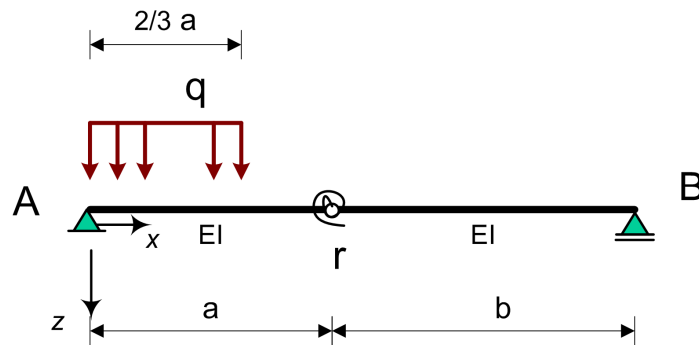


Figure 3 : Beam structure with rotational spring and (partially) distributed load.

**Questions:**

- The value of the spring stiffness is of influence of the maximum moment in the structure?
- Find the (absolute) value of the support reaction at  $A$  in kN.
- Find the (absolute) value of the kink in the beam at the location of the spring in radians.
- Find the amount of energy stored due to bending deformation in this structure in Joule.
- Find the vertical displacement of the connection between the two beam parts using Castigliano's theoreme.