

Opmerkingen: Zie §4.4, blz. 150 t/m 153
 Zie §4.5.4, blz. 160 t/m 163

Antwoorden:

- a. $F_p = 2000 \text{ kN}$
 b. $\sigma_b = -8,88 \text{ N/mm}^2$ en $\sigma_o = 0$

Toelichting:

$$A = 450 \times 10^3 \text{ mm}^2 \text{ en } I_{zz} = 30,375 \times 10^9 \text{ mm}^4$$

a. In de middendoorsnede:

$$\text{t.g.v. } q: \quad M = \frac{1}{8}(100 \text{ kN/m})(8 \text{ m})^2 = 800 \text{ kNm}$$

$$\text{t.g.v. } F_p: \quad M = -F_p e_p = -F_p(0,25 \text{ m})$$

$$\text{verder:} \quad N = -F_p$$

$$\sigma_o = \frac{-F_p}{450 \times 10^{-3} \text{ m}^2} + \frac{((800 \text{ kNm}) - F_p(0,25 \text{ m}))(0,45 \text{ m})}{30,375 \times 10^{-3} \text{ m}^4} \leq 0$$

$$\Rightarrow F_p \geq 2000 \text{ kN}$$

b. Ten gevolge van voorspankracht:

$$N = -2 \times 10^6 \text{ N en } M = (-2 \times 10^6 \text{ N})(250 \text{ mm}) = -500 \times 10^6 \text{ Nmm}$$

$$\sigma^{(N)} = \frac{-2 \times 10^6 \text{ N}}{450 \times 10^3 \text{ mm}^2} = -4,44 \text{ N/mm}^2$$

$$\sigma_b^{(M)} = \frac{(-500 \times 10^6 \text{ Nmm})(-450 \text{ mm})}{3,0375 \times 10^{10} \text{ mm}^2} = +7,41 \text{ N/mm}^2$$

$$\sigma_o^{(M)} = \frac{(-500 \times 10^6 \text{ Nmm})(+450 \text{ mm})}{3,0375 \times 10^{10} \text{ mm}^2} = -7,41 \text{ N/mm}^2$$

Ten gevolge van de verdeelde belasting:

$$M = +800 \times 10^6 \text{ Nmm}$$

$$\sigma_b^{(M)} = \frac{(+800 \times 10^6 \text{ Nmm})(-450 \text{ mm})}{3,0375 \times 10^{10} \text{ mm}^2} = -11,85 \text{ N/mm}^2$$

$$\sigma_o^{(M)} = \frac{(+800 \times 10^6 \text{ Nmm})(+450 \text{ mm})}{3,0375 \times 10^{10} \text{ mm}^2} = +11,85 \text{ N/mm}^2$$