

Remarks: See §2.6, pages 34 till 42

Answers:

- a. $q = 50 \text{ kN/m}$
 b. $\Delta \ell = -20,8 \text{ mm}$

Explanation:

$$EA = 2,25 \times 10^6 \text{ kN}$$

$$\text{a. } q = \frac{(2550 \text{ kN}) - (1350 \text{ kN})}{24 \text{ m}} = 50 \text{ kN/m}$$

$$\text{b. } \Delta \ell = \int_0^{\ell} \frac{N(x) dx}{EA} \text{ where } N(x) = -F_1 + qx$$

Working out this equation analytically gives the answer.

- b. Alternative: Draw the N-diagram. The slope of the diagram is linear going from $N = -F_1 = -2550 \text{ kN}$ at the top of the pile to $N = -F_2 = -1350 \text{ kN}$ at the bottom.

$$\begin{aligned} \Delta \ell &= \frac{1}{EA} \int_0^{\ell} N(x) dx = \frac{\text{Area under } N\text{-diagram}}{EA} = \\ &= \frac{\frac{1}{2} \times \{(-2550 \text{ kN}) + (-1350 \text{ kN})\} (24 \text{ m})}{2,25 \times 10^6 \text{ kN}} = -20,8 \times 10^{-3} \text{ m} \end{aligned}$$