

Remarks: See §3.1.4, example 3, pages 85 till 86

See §3.3.2, example 2, pages 126 till 129

Answers:

a. $A = 2Rt\alpha$

b. $S_y = 2R^2t \sin \alpha$

$S_z = 0$

c. $y_C = \frac{R \sin \alpha}{\alpha}$

$z_C = 0$

d. $I_{yy} = \frac{R^3t}{2}(2\alpha + \sin 2\alpha)$

$I_{zz} = \frac{R^3t}{2}(2\alpha - \sin 2\alpha)$

$I_{yz} = I_{zy} = 0$

e. $I_{yy;centr} = \frac{R^3t}{2}(\sin 2\alpha + 2\alpha) - \frac{2R^3t \sin^2 \alpha}{\alpha}$

$I_{zz;centr} = \frac{R^3t}{2}(2\alpha - \sin 2\alpha)$

$I_{yz;centr} = I_{zy;centr} = 0$

$\alpha = \frac{\pi}{2}$ (half ring):

$A = \pi Rt$; $S_y = 2R^2t$; $S_z = 0$

$y_C = \frac{2R}{\pi}$ and $z_C = 0$

$I_{yy} = I_{zz} = \frac{\pi R^3t}{2}$ and $I_{yz} = I_{zy} = 0$

$I_{yy;centr} = \left(\frac{\pi}{2} - \frac{4}{\pi}\right)R^3t$ and $I_{zz;centr} = \frac{\pi R^3t}{2}$

$I_{yz;centr} = I_{zy;centr} = 0$

$\alpha = \pi$ (complete ring):

$A = 2\pi Rt$; $S_y = S_z = 0$

$y_C = z_C = 0$

$I_{yy} = I_{zz} = \pi R^3t$ and $I_{yz} = I_{zy} = 0$

$I_{yy;centr} = I_{zz;centr} = \pi R^3t$

$I_{yz;centr} = I_{zy;centr} = 0$