

Remarks: See §4.4, pages 168 till 170

See §4.5.4, pages 179 till 182

Hints:

Schematize the beam as a line element and draw all the forces and couples that act on this line.

Answers:

b. In cross-sections B and C.

$$\sigma_t = +1,52 \text{ N/mm}^2 \text{ and } \sigma_b = -14,13 \text{ N/mm}^2$$

c. In cross-section E.

$$\sigma_t = -9,97 \text{ N/mm}^2 \text{ and } \sigma_b = +1,95 \text{ N/mm}^2$$

d. 98 mm

Explanation:

a. The pre-stressing tendon applies eccentric compressive forces on the beam ends. This causes a normal force and a bending moment:

$$N = -1200 \text{ kN}; \quad M_z = Ne = (-1200 \text{ kN})(0,09 \text{ m}) = -108 \text{ kNm}$$

b. At the cross-sections of B and C:

$$N = -1200 \text{ kN}; \quad M_z = (-108 \text{ kNm}) + (-85 \text{ kNm}) = -193 \text{ kNm}$$

$$\sigma^{(N)} = -5 \text{ N/mm}^2; \quad \sigma_t^{(M)} = +6,52 \text{ N/mm}^2; \quad \sigma_b^{(M)} = -9,13 \text{ N/mm}^2$$

c. At cross-section E:

$$N = -1200 \text{ kN}; \quad M_z = (-108 \text{ kNm}) + (+255 \text{ kNm}) = +147 \text{ kNm}$$

$$\sigma^{(N)} = -5 \text{ N/mm}^2; \quad \sigma_t^{(M)} = -4,97 \text{ N/mm}^2; \quad \sigma_b^{(M)} = +6,95 \text{ N/mm}^2$$

$$d. \quad a = \frac{1,95}{1,95 + 9,97} \times 600 = 98 \text{ mm}$$