

Remarks: See §5.4.3, example 2, pages 350 till 355

See §6.2, pages 415 till 426

See §6.3.1, pages 427 till 437

Answer:

- a. $\tau = 6,25 \text{ N/mm}^2$
- b. $\tau_{\max} = 2,5 \text{ N/mm}^2$
- c. $\tau_{\max} = 8,75 \text{ N/mm}^2$
- d. $\sigma_{\max} = 25,6 \text{ N/mm}^2$

Explanation:

Loads in cross-section A:

$$M_t = 15,7 \text{ kNm}; V = 15,7 \text{ kN}; M = 31,4 \text{ kNm}; N = 0$$

Cross-section properties:

$$I_p = 160\pi \times 10^6 \text{ mm}^4, I = \frac{1}{2} I_p = 80\pi \times 10^6 \text{ mm}^4;$$

$$A_m = 40\pi \times 10^3 \text{ mm}^2$$

$$\text{For half-section: } S^a = z^a \cdot A^a = \frac{2R}{\pi} \cdot \pi R t = 800 \times 10^3 \text{ mm}^3$$

$$\text{a. } \tau = \frac{M_t r}{I_p} = \frac{(15,7 \times 10^6 \text{ Nmm})(200 \text{ mm})}{160\pi \times 10^6 \text{ mm}^4} = 6,25 \text{ N/mm}^2, \text{ of}$$

$$\tau = \frac{M_t}{2A_m t} = \frac{15,7 \times 10^6 \text{ Nmm}}{2 \times (40\pi \times 10^3 \text{ mm}^2)(10 \text{ mm})}$$

- b. On the vertical line of symmetry $\tau = 0$.

The maximum shear stress is at the height of the normal centre:

$$\tau_{\max} = \frac{VS^a}{b^a I} = \frac{(15,7 \times 10^3 \text{ N})(800 \times 10^3 \text{ mm}^3)}{(20 \text{ mm})(80\pi \times 10^6 \text{ mm}^4)} = 2,5 \text{ N/mm}^2$$

- c. At the left side of the tube the shear stress due to shear force and torsional moment act in the same direction:

$$\tau_{\max} = 6,25 \text{ N/mm}^2 + 2,5 \text{ N/mm}^2 = 8,75 \text{ N/mm}^2.$$

$$\text{d. } \sigma_{\max} = \frac{(31,4 \times 10^6 \text{ Nmm})(205 \text{ mm})}{80\pi \times 10^6 \text{ mm}^4} = 25,6 \text{ N/mm}^2$$

Tension in the upper side and compression in the lower side.