

Remarks: See §5.4.3 pages 345 till 355

See §6.3.1, pages 427 till 437

See §6.4, example 5 till 8, pages 458 till 468

Answers:

a. $\tau_{\max; \text{flange}} = 0,68 \text{ N/mm}^2 \quad \tau_{\max; \text{web}} = 1,69 \text{ N/mm}^2$

(τ constant over the wall thickness)

b. open cross-section (τ varies linearly over the wall thickness):

$$\tau_{\max; \text{flange}} = 7 \text{ N/mm}^2 \quad \tau_{\max; \text{web}} = 3,5 \text{ N/mm}^2$$

Closed cross-section (τ constant over the wall thickness):

$$\tau_{\text{flange}} = 0,16 \text{ N/mm}^2 \quad \tau_{\text{web}} = 0,32 \text{ N/mm}^2$$

c. open cross-section: $\tau_{\max} = 7,68 \text{ N/mm}^2$

d. Closed cross-section: $\tau_{\max} = 2,01 \text{ N/mm}^2$

Explanation:

$$V_z = 3,78 \times 10^3 \text{ N} ; M_t = 1,512 \times 10^3 \text{ Nmm}$$

Open CS.: $I_{zz} = 56 \times 10^6 \text{ mm}^4$; $I_t = 259,2 \times 10^3 \text{ mm}^4$ (strip)

Closed CS.: $I_{zz} = 56 \times 10^6 \text{ mm}^4$; $A_m = 40 \times 10^3 \text{ mm}^2$ (Bredt)

a. The shear stress in the flanges varies linearly:

$$\tau_{\max} = \frac{(3,78 \times 10^3 \text{ N})(240 \times 10^3 \text{ mm}^3)}{(2 \times 12 \text{ mm})(56 \times 10^6 \text{ mm}^4)} = 0,68 \text{ N/mm}^2$$

The shear stress distribution in the webs is parabolic:

$$\tau_{\max} = \frac{(3,78 \times 10^3 \text{ N})(300 \times 10^3 \text{ mm}^3)}{(2 \times 6 \text{ mm})(56 \times 10^6 \text{ mm}^4)} = 1,69 \text{ N/mm}^2$$

b. Torsion open cross-section:

$$\tau_{\max; \text{flange}} = \frac{(151,2 \times 10^3 \text{ Nmm})(6 \text{ mm})}{\frac{1}{2} \times (259,2 \times 10^3 \text{ mm}^4)} = 7 \text{ N/mm}^2$$

$$\tau_{\max; \text{web}} = \frac{(151,2 \times 10^3 \text{ Nmm})(3 \text{ mm})}{\frac{1}{2} \times (259,2 \times 10^3 \text{ mm}^4)} = 3,5 \text{ N/mm}^2$$

Torsion closed cross-section (Bredt's formula):

$$\tau_{\text{flange}} = \frac{151,2 \times 10^3 \text{ Nmm}}{2 \times (40 \times 10^3 \text{ mm}^2)(12 \text{ mm})} = 0,16 \text{ N/mm}^2$$

$$\tau_{\text{web}} = \frac{151,2 \times 10^3 \text{ Nmm}}{2 \times (40 \times 10^3 \text{ mm}^2)(6 \text{ mm})} = 0,32 \text{ N/mm}^2$$

c. $\tau_{\max} = 7,68 \text{ N/mm}^2$; in the upper flange bottom left and top right;
in the bottom flange top left and bottom right

d. $\tau_{\max} = 2,01 \text{ N/mm}^2$; in the right web at the height of the NC.